

Higgs Physics with a $\gamma\gamma$ Collider Based on CLIC 1

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Abstract

We present the machine parameters and physics capabilities of the CLIC Higgs Experiment (CLICHE), a low-energy $\gamma\gamma$ collider based on CLIC 1, the demonstration project for the higher-energy two-beam accelerator CLIC. CLICHE is conceived as a factory capable of producing around 20,000 light Higgs bosons per year. We discuss the requirements for the CLIC 1 beams and a laser backscattering system capable of producing a $\gamma\gamma$ total (peak) luminosity of $2.0 (0.36) \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ with $E_{CM}(\gamma\gamma) \sim 115 \text{ GeV}$. We show how CLICHE could be used to measure accurately the mass, $b\bar{b}$, WW and $\gamma\gamma$ decays of a light Higgs boson. We illustrate how these measurements may distinguish between the Standard Model Higgs boson and those in supersymmetric and more general two-Higgs-doublet models, complementing the measurements to be made with other accelerators. We also comment on other prospects in $\gamma\gamma$ and $e^- \gamma$ physics with CLICHE.

1 Introduction

CLIC [1] is a project for a multi-TeV linear e^+e^- collider using an innovative two-beam acceleration technique to achieve a high accelerating gradient, and CLIC 1 [2] is an essential step proposed at CERN in the R&D programme towards CLIC. CLIC 1 would be based on one module of the eventual full CLIC accelerator, capable of delivering an intense, low-emittance e^- beam with an energy ~ 70 GeV. CLIC 1 is required to provide proof-of-principle for the two-beam acceleration mechanism of CLIC on a large scale, and would represent a major investment in engineering and other resources. It is natural to seek to maximize the physics return on this investment.

Several possible uses of an intense e^- beam are readily apparent. One could in principle use it for *fixed-target experiments*, for example. One could envision *colliding CLIC 1 with the LHC proton beam*, but the orientation and depth of CLIC 1 that would be required are not compatible with the possibility of extending CLIC 1 subsequently to become the full CLIC machine. If one had two CLIC 1 machines, a positron source and damping rings, one could make e^+e^- collisions. There has recently been a resurgence of physics interest in a new round of high-statistics experiments at the Z^0 peak, *GigaZ* [3, 4, 5], aimed at higher-precision electroweak measurements. The centre-of-mass energy range $\sim m_Z$ would certainly be within range of a pair of CLIC 1 machines, but effectiveness of the *GigaZ* programme would require the positrons to be polarized, as well as the electrons, which is a technical challenge. There is also interest in returning to *the $e^+e^- \rightarrow W^+W^-$ threshold*, in order to measure m_W more precisely. The W^+W^- threshold would be within reach of a modest upgrade of the nominal CLIC 1 energy.

Alternatively, with two CLIC 1 machines, or even just one feeding two arcs à la SLC, and a laser backscattering laser facility to produce high-energy photons by the Compton process $e^-\gamma_{laser} \rightarrow e^-\gamma$. One could make $e^-\gamma$ and/or $\gamma\gamma$ collisions at centre-of-mass energies up to ~ 0.9 or $\sim 0.8 \times E_{CM}(e^-e^-)$, respectively. A polarized positron source would not be needed for such experiments. The principles of photon colliders [6] and the physics interest of $\gamma\gamma$ collisions, in particular, have been documented extensively [7, 8].

Precision electroweak fits suggest [9] that the most likely mass for the Standard Model Higgs boson is just above the limit of 114 GeV provided by direct searches at LEP [10]. Moreover, the mass range $m_H \lesssim 130$ GeV [11] is suggested independently by supersymmetry. We also recall that the last days of LEP even provided a direct hint for a Standard Model-like Higgs boson with mass ~ 115 GeV [10], and that LEP could not exclude a supersymmetric Higgs boson as light as ~ 90 GeV. The possibility of such a light Higgs boson may be confirmed or refuted by the Tevatron collider within a few years, and the LHC would certainly measure the value of m_H . With the injection energy of 9 GeV, the nominal energy of CLIC 1 is 77 GeV. Therefore, the effective $E_{CM}(\gamma\gamma)$ could be tuned to a value up to $\sim 0.8 \times 154$ GeV ~ 120 GeV.

Thus there exists an opportunity for turning CLIC 1 into a Higgs factory, a proposal we term the CLIC Higgs Experiment, or CLICHE. As discussed in [12], the option of colliding the beams from two CLIC 1 machines looks promising, and the geometric e^-e^- luminosity may attain around $4.8 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$. Combined with a suitable laser backscattering system, such

a luminosity would enable accurate measurements of the properties of the Higgs boson. For example, the laser system described below could yield a total $\gamma\gamma$ luminosity of up to 200 fb^{-1} per ‘Snowmass year’ of 10^7 s, which could produce around 22,000 light Standard Model (SM) Higgs particles.

In subsequent sections of this paper, we first assemble some initial considerations of accelerator aspects of CLICHE, including the requirements for the CLIC 1 beam parameters and the laser system if one is to attain a luminosity sufficient to study Higgs physics. Then we review briefly some of the most interesting physics measurements possible with CLICHE, which could include accurate measurements of m_H , $\Gamma(H \rightarrow \gamma\gamma) \times \mathcal{B}r(H \rightarrow \bar{b}b)$, $\Gamma(H \rightarrow \gamma\gamma) \times \mathcal{B}r(H \rightarrow WW)$, $\Gamma(H \rightarrow \gamma\gamma) \times \mathcal{B}r(H \rightarrow \gamma\gamma)$, and the CP properties of the $H \rightarrow \gamma\gamma$ coupling. We study the capability of CLICHE to distinguish a Standard Model Higgs from the lightest Higgs boson in the minimal supersymmetric extension of the Standard Model (MSSM), and also discuss a more general two-Higgs-doublet model.

As we also mention, there are other physics processes that might be interesting at CLICHE, *e.g.*, QCD reactions in $\gamma\gamma$ collisions and the reaction $e^-\gamma \rightarrow \nu W^-$ in $e^-\gamma$ collisions, which would provide an opportunity to measure m_W and Γ_W . We also advertise the physics opportunities for Higgs physics offered by higher-energy $\gamma\gamma$ colliders, for which CLICHE might serve as an engineering prototype. For example, the study of higher-mass Higgs bosons may best be done at high-energy $\gamma\gamma$ colliders, due to the fact that they are produced in the s channel (so that all of the phase space is available for producing the Higgs mass) [13, 14], and the fact that the photon beams can be produced in a state of definite CP.

2 Accelerator Considerations

This section describes two important components of CLICHE, namely the CLIC 1 electron accelerator and the laser backscattering system.

At CERN, a high energy, high luminosity electron-positron linear collider (CLIC for Compact Linear Collider) is being studied as a possible post-LHC facility [1]. It is based on a novel two-beam scheme and uses high-frequency, high-gradient normal-conducting structures to accelerate the beam. The power to accelerate this main beam is obtained by decelerating drive beams in a dedicated beam line passing parallel to the main linac. CLIC requires two drive-beam complexes, each of which generate the 22 drive-beam pulses necessary to power 22 drive-beam decelerators for one of the two main linacs, for e^+e^- collisions at 3 TeV centre-of-mass energy. The two-beam acceleration has been demonstrated successfully in two test facilities (CTF1 and CTF2). A test of the drive-beam generation will take place at a new test facility (CTF3) [15], presently under construction. Its operation will enable one to judge whether the technology works, and it is expected that a conceptual design report for CLIC could be completed by the end of 2006. CTF3 should be followed by CLIC 1, which is conceived to provide a full scale test of beam dynamics and power handling.

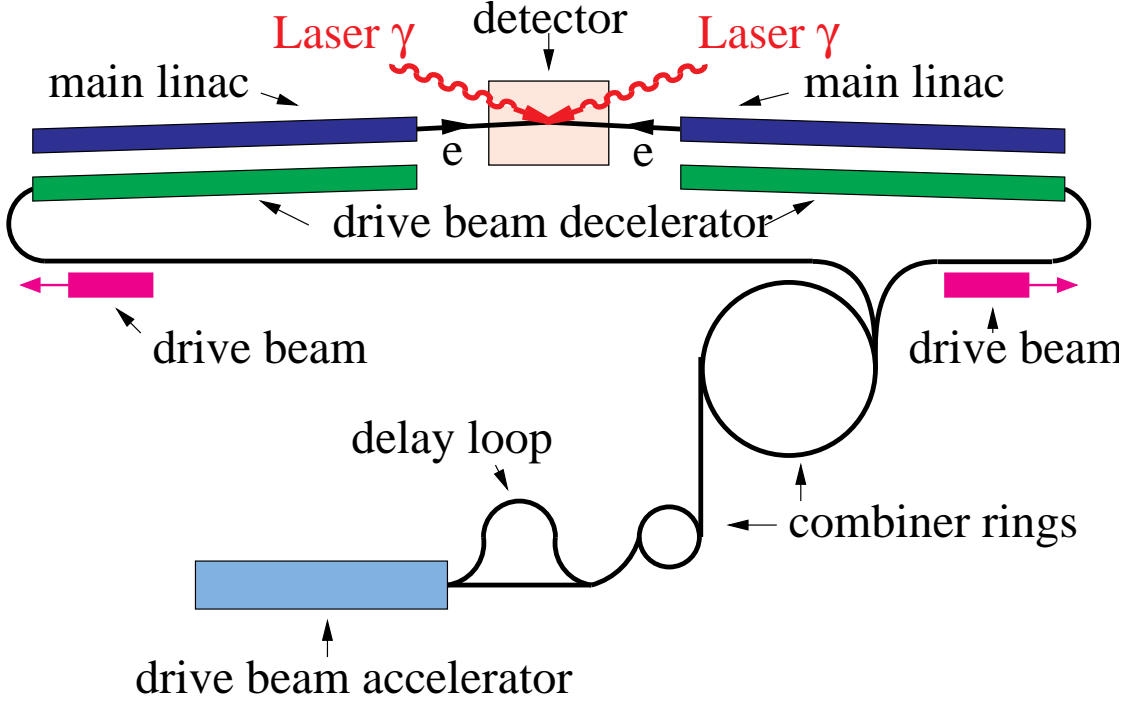


Figure 1: *Schematic sketch of a layout for a $\gamma\gamma$ collider based on CLIC 1.*

2.1 Parameters of CLIC 1

CLIC 1 is proposed to consist of one drive-beam generation complex and one drive-beam decelerator, with the corresponding length of main linac sufficient to accelerate a main beam by about 68 GeV.

Recently, an exploratory study has been carried out to determine how this facility could be turned into a collider with a high geometric e^-e^- luminosity, which could be used as the basis for a $\gamma\gamma$ collider [12]. This would require the addition of a small-emittance main-beam source and a final-focus system able to achieve small spot sizes at the interaction point (IP). In addition, it would be necessary to achieve a high beam current in the main linac. The main linac of CLIC 1 could in principle be turned into a collider by adding arcs as in SLC [16]. However, it seems simpler to add a second CLIC 1 linac pointing at the first one, and only this option is considered here. Some preliminary parameters of a potential e^-e^- collider are given in Table 1. A more detailed investigation is required in order to establish the feasibility of the approach and to find possible improvements.

In the proposed CLIC 1 collider scheme, the CLIC drive-beam complex can power both linacs. Alternate pulses are sent into the first and second linac, as seen in Fig. 1. The two pulses accelerate the main beams at the same time if the drive-beam complex is properly placed. The third pulse can be used to power again the first linac and the fourth to power the second, and so on, using all drive-beam pulses. This effectively increases the repetition frequency from

100 Hz to 1.1 kHz. However, it remains to be investigated if the structures can tolerate the heat load associated with this mode of operation. A repetition frequency of 200 Hz is foreseen for CLIC at a centre-of-mass energy of 500 GeV. The effective repetition frequency that we assume is therefore in the range of 200–1100 Hz depending on the heat load capabilities of the structures. This leads to an uncertainty in the final luminosity by a factor of five.

In the preferred two-beam scheme, the main beams would be generated by a conventional electron source, which could provide a polarization of about 80%. The injector could likely use the slightly modified SPS as a damping ring [17, 18]. The beams would be accelerated to 9 GeV before injection into the main linac, increasing the maximum beam energy to ~ 77 GeV. After the linac, a collimation system would scrape off the beam tails, and a final-focus system would focus the beams down to about 2.9 nm vertically and 154 nm horizontally.

The geometric e^-e^- luminosity that may be achievable is $\mathcal{L} \simeq (4 \times 10^9 \times 4 \times 10^9 / 154 \times 10^{-7} / 2.9 \times 10^{-7})(100 \times 11 \times 154 / 4 / 3.1415) = 4.8 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ and $\mathcal{L} \simeq 0.9 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ for an effective repetition rate of 1.1 kHz and 200 Hz, respectively. It may be possible to increase the luminosity by using a larger bunch charge and by decreasing the vertical emittance, and further study is needed to find the limits of these parameters.

Table 1: *Example parameters for a CLIC 1 collider.*

variable	symbol	value
total power consumption for RF	P	150 MW
beam energy	E	75 GeV
beam polarization	P_e	0.80
bunch population	N	4×10^9
number of bunches per train	n_b	154
number of trains per rf pulse	n_t	11
repetition rate	f_{rep}	100 Hz
rms bunch length	σ_z	30 μm
crossing angle	θ_c	≥ 20 mrad
normalised horizontal emittance	ϵ_x	1.4 μm
normalised vertical emittance	ϵ_y	0.05 μm
nominal horizontal beta function at the IP	β_x^*	2 mm
nominal vertical beta function at the IP	β_y^*	20 μm
e^-e^- geometric luminosity	\mathcal{L}	$0.9\text{--}4.8 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$

2.2 Laser Backscattering System

The photon beams required by CLICHE would be produced via the Compton backscattering of laser light off the high-energy electron beam from CLIC 1. The bunch-to-bunch distance and pulse length of CLICHE are of the same order of magnitude as those for NLC. The laser

requirements for CLIC and NLC are therefore comparable, since they both use all the Mercury technologies¹ - pump diodes, Yb-SFAP crystals, cooling, chirp pulse, etc. [7], the only differences being at the front end. On the other hand, the TESLA option [8] requires a high-speed lower-power optical switch (Pockels cell) which is under development at LLNL.

In the laser-beam collision at the conversion point, the maximum energy of the scattered photons is:

$$\omega_m = \frac{x}{x+1}E_0; \quad x \approx \frac{4E_0\omega_0}{m^2c^4} \simeq 15.3 \left[\frac{E_0}{\text{TeV}} \right] \left[\frac{\omega_0}{\text{eV}} \right], \quad (1)$$

where E_0 is the electron beam energy and ω_0 the energy of the laser photon. In connection with NLC studies [7], the case $E_0 = 250$ GeV, $\omega_0 = 1.17$ eV, i.e., $\lambda = 1.0$ μm , has been considered. This would correspond to $x = 4.5$ and $\omega_m = 0.82E_0$. In the case of CLICHE, the centre-of-mass energy of the accelerator would be $E_{CM}(e^-e^-) \simeq 150$ GeV. In order for $E_{CM}(\gamma\gamma)$ to be close to the mass of a 115 GeV Higgs boson, the energy of the laser photon is chosen to be 3.53 eV instead of 1.17 eV, resulting in a maximum photon energy of roughly 60 GeV.

We need to add frequency multipliers to reduce the wavelength. The increase in the laser frequency is achieved by adding a tripler to the laser system. In this case it can be assumed that the 1.054 μm laser can be turned into one with 0.351 μm . As a consequence, the power provided by the photons is reduced by a factor 1/3. However the area of the focal spot is also reduced by 1/3, so the overall effect cancels out in the power in the peak. A 70% tripling efficiency is expected. Parameters of the electron and laser beams are shown in Table 1 and 2. We find that CLICHE requires between $154 \times 2 \times 100 = 30800$ and $154 \times 11 \times 100 = 169400$ pulses/second. As a consequence, the use of more elaborate multi-pass optics than the two-pass system designed for NLC [7] would be important for reducing the required number of laser pulses.

The optimum polarization combination that we anticipate for the electron beam P_e and the laser beam P_L is $P_e P_L = -0.8$. In this case the generated photon spectrum peaks at its maximum energy, ω_m . In addition, the high-energy photon beam is almost completely polarized around the peak energy. In order to enhance the Higgs production and to suppress the background events, from $\gamma\gamma \rightarrow \bar{b}b + ng$ in particular, the polarizations of the colliding photon beams should be arranged so that $J_z = 0$ collisions dominate. With the CLIC 1 beam energy, the Higgs particle of 115 GeV is produced almost at rest, while the low-energy background events are strongly boosted. Hence the backgrounds will in general have topologies that are different from the desired signal events, as discussed later.

The expected total energy spectra and polarization are shown in Fig. 2. The luminosity calculation assumes improvements over what was originally proposed in [12]:

- use of the most recent NLC Final-Focus System (FFS) for operation of the center-of-mass of 0.5-1 TeV [19],

¹This laser technology is capable of delivering the 10 kW of average power in short pulses of 1 TW peak power. The total energy of a pulse is 1 J.

Table 2: *Example of laser parameters for a $\gamma\gamma$ collider based on CLIC 1 for $\mathcal{L}_{ee} = 4.8 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$.*

variable	symbol	value
Laser beam parameters		
Wavelength	λ_L	$0.351 \mu\text{m}$
Photon energy	$\hbar\omega_L$	$3.53 \text{ eV} = 5.65 \times 10^{-19} \text{ J}$
Number of laser pulses per second	N_L	169400 s^{-1}
Laser peak power	W_L	$2.96 \times 10^{22} \text{ W/m}^2$
Laser peak photon density		$5.24 \times 10^{40} \text{ photons/m}^2/\text{s}$
Photon beam		
Number of photons per electron bunch	N_γ	9.6×10^9
$\gamma\gamma$ luminosity	$\mathcal{L}_{\gamma\gamma}$	$2.0 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
$\gamma\gamma$ luminosity for $E_{\gamma\gamma} \geq 0.6E_{CM}$	$\mathcal{L}_{\gamma\gamma}^{peak}$	$3.6 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$

- and increasing the strength of the bending magnets by a factor of 4.35, with corresponding decreases in the sextupole, octupole and decapole strengths by 4.35, 4.35^2 and 4.35^3 . This allows the beta functions to be reduced from the NLC values: $\beta_x=2 \text{ mm}$ (previously 8 mm) and $\beta_y=20 \mu\text{m}$ (previously $100 \mu\text{m}$).

Tracking simulations of the FFS that take into account the synchrotron radiation in the dipoles and quadrupoles and the initial beam energy distribution from the linac as simulated with DIMAD [20] and PLACET [21] predict a geometric luminosity of roughly $4.8 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ for 11 trains per rf pulse. The energy spread was assumed to be $\Delta E/E \sim 0.23\%$. The horizontal and vertical normalized emittances were taken to be $1.4 \times 10^{-6} \text{ m}$ and $5 \times 10^{-8} \text{ m}$, respectively, and the RMS at the IP is 138.1 nm (2.6 nm) in the horizontal (vertical) plane. However, DIMAD predicts that the effective beam spot is larger, $(154 \times 2.9) \text{ nm}^2$. This is due to effects such as synchrotron radiation and the combination of chromaticity of the FFS and the electron beam energy spread. As a consequence, the luminosity is simulated to be 15% lower than the ‘ideal’ scenario. These effects are taken into account in the luminosity results shown in Fig. 2. Using the laser parameters described above, the $\gamma\gamma$ luminosity with a centre-of-mass energy above $0.6 \times 150 \text{ GeV}$ is about $3.6 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$, and the polarization $\langle \lambda\lambda' \rangle$ at the peak is 0.94.

We have chosen the distance between the conversion point and the interaction point to be 1 mm . Detailed studies indicate that the optimal value is 1.4 mm , which would yield a somewhat higher luminosity. On the other hand, there would be a reduction in luminosity if a more conservative beam spot size were assumed, so we consider the figures presented here quite representative.

The laser-beam collision at the conversion point and the beam-beam collision at the interaction point have been simulated using CAIN [26] and using GUINEA-PIG [22]. The results of the two programs agree quite well. The luminosity spectra and the effective beam polarization as functions of $E_{CM}(\gamma\gamma)$ obtained using CAIN are shown in Fig. 2. Both of these need to be

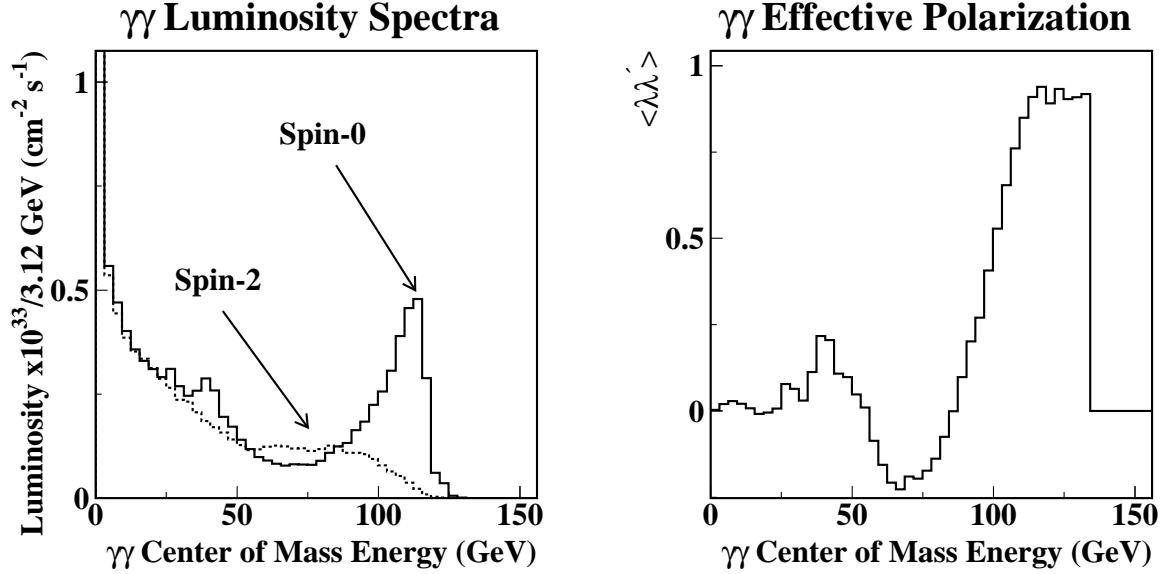


Figure 2: *Luminosity spectra and beam polarization as functions of $E_{CM}(\gamma\gamma)$ for the CLIC 1 parameters for 75 GeV electrons obtained with DIMAD [20] and CAIN [26] for $\mathcal{L}_{ee} = 4.8 \times 10^{34} \text{cm}^{-2} \text{s}^{-1}$.*

monitored and controlled accurately. At the E_{CM} under consideration, the spectra and luminosity can be measured using the reaction $\gamma\gamma \rightarrow e^+e^-$ [23]. The reaction $\gamma\gamma \rightarrow e^+e^-\gamma$ may also be useful for this purpose, but this requires further study. The polarization cannot be measured using the reaction $\gamma\gamma \rightarrow \mu^+\mu^-\mu^+\mu^-$ as originally suggested [23]. A promising way of measuring the photon polarization uses the reactions $e\gamma \rightarrow e\gamma$ and $e\gamma \rightarrow W\nu$. A detailed study of the second process in which the full photon energy spectrum is taken into account is in progress [24]. Fig. 3 displays the variation of the cross section with the photon polarization, together with the attainable statistical error. The latter would correspond to a determination of the photon polarization with a precision of $\pm 1\%$.

3 Physics Opportunities

Our primary thrust in this paper is to emphasize the Higgs physics accessible with CLICHE. However, there are other interesting physics opportunities, as we discuss in the last two subsections.

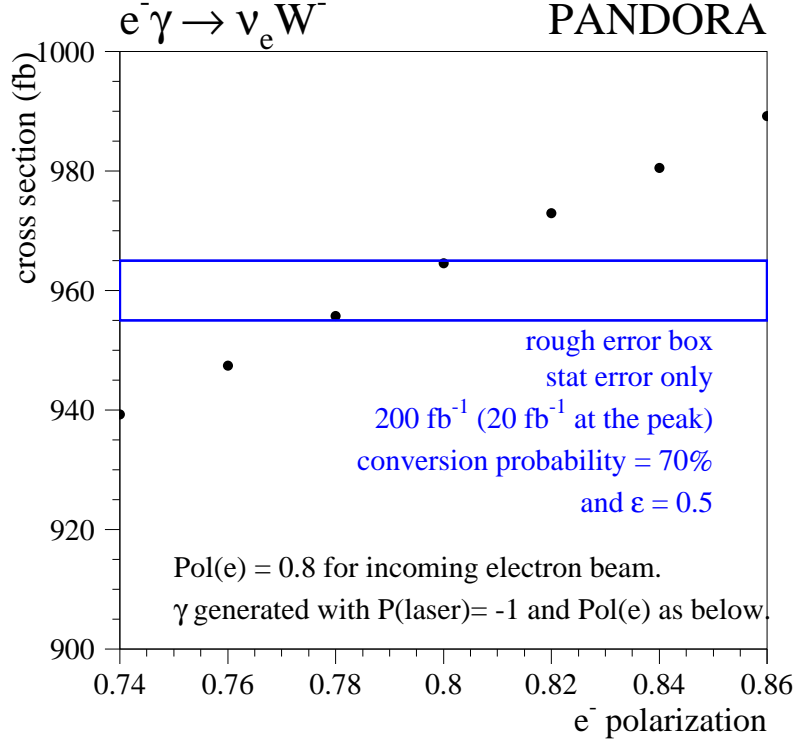


Figure 3: *The variation in the cross section for the $e\gamma \rightarrow W\nu$ process as a function of polarization. This analysis includes the full photon spectrum in the cross section calculation. The attainable statistical error in the cross-section measurement is also indicated.*

3.1 A Higgs Factory

There have been many investigations of the physics possibilities of $\gamma\gamma$ colliders, including discussions of $\gamma\gamma$ options at JLC [25], NLC [7] and TESLA [8]. Here we describe results from exploratory studies of a $\gamma\gamma$ collider optimized for a light Higgs factory scenario at CLIC 1. As discussed in some detail below, several important measurements of Higgs properties can be made at a Higgs factory. In fact, for many of the analyses, running close to the Higgs threshold has important advantages.

We begin with a discussion of the Higgs production cross section. The excitation curve for a Higgs boson with mass around 115 GeV as a function of $E_{CM}(e^-e^-)$ for unpolarized electrons is shown in Fig. 4(a). We see that the cross section rises rapidly for $E_{CM}(e^-e^-)$ between 140 and 160 GeV, providing a physics opportunity for CLIC 1 with a beam energy of 77 GeV, if indeed $m_H \sim 115$ GeV. Fig. 4(b) shows the cross section as a function of Higgs mass for three choices of $E_{CM}(e^-e^-)$. We note that the excitation curve increases by a factor of three if the electron beams are 80% longitudinally polarized. The CLIC 1 energy could be somewhat lower if the lower limit of about 90 GeV on the lightest MSSM Higgs mass is saturated, whereas an energy upgrade would be required if the MSSM upper bound of about 130 GeV were to be

saturated.

The most important decay modes of a Standard Model Higgs boson in the range between 100 and 200 GeV are shown in Fig. 5. We see that the $H \rightarrow \gamma\gamma$ coupling used to produce the Higgs boson at CLICHE yields a relatively minor decay mode, whereas the dominant decay mode for a Standard Model Higgs boson weighing ~ 115 GeV is $H \rightarrow b\bar{b}$. Indeed, the most promising reaction at such a Higgs factory is $\gamma\gamma \rightarrow H \rightarrow b\bar{b}$, as we discuss below. Other decay channels accessible at CLICHE include $H \rightarrow WW$ and $H \rightarrow \gamma\gamma$. In the Standard Model, the branching ratios for $\mathcal{B}r(H \rightarrow b\bar{b})$, $\mathcal{B}r(H \rightarrow WW)$ and $\mathcal{B}r(H \rightarrow \gamma\gamma)$ for a Higgs mass of 115 GeV are: 73.7%, 8.8% and 0.2%, respectively. One of the objectives of CLICHE would be to test these predictions, and use measurements of them to distinguish between the Standard Model and its possible extensions, such as the minimal supersymmetric extension of the Standard Model (MSSM) or a more general two-Higgs-doublet model (2HDM), as we discuss later.

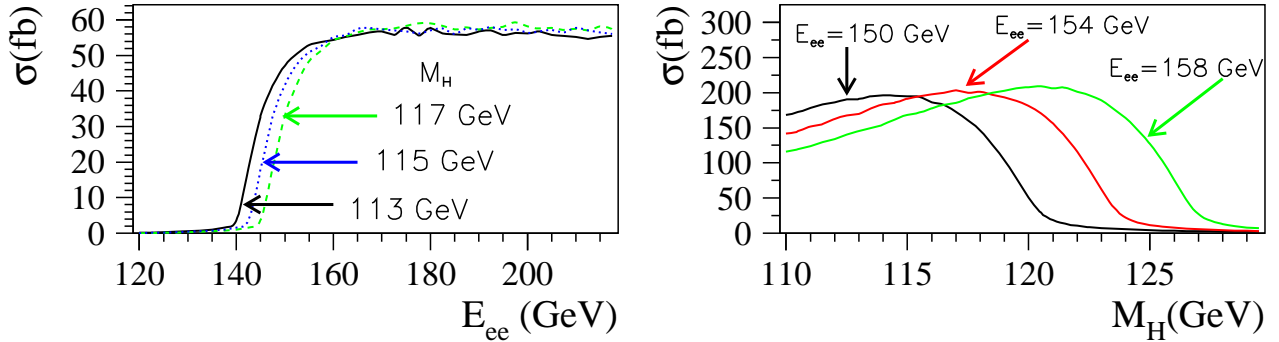


Figure 4: (a) The cross sections for $\gamma\gamma \rightarrow H$ for different values of m_H as functions of $E_{CM}(e^-e^-)$ for unpolarized photons. (b) The cross section for $\gamma\gamma \rightarrow H$ as a function of m_H for three different values of $E_{CM}(e^-e^-)$. Here the electrons are assumed to be 80% polarized longitudinally, and the lasers circularly polarized, so that the produced photons are highly circularly polarized at their maximum energy.

3.1.1 Higgs measurements with CLICHE

In all the studies shown below, realistic beam spectra and luminosities were used. The calculations were based on the **CAIN** program [26] which includes the non-linear effects that can cause distortions in the photon beam energy spectra, as well as the latest description of the interaction region. The photon helicities were taken into account in the signal and background estimations. The events were generated using **PANDORA-PYTHIA** [27, 28], and **LCDROOT FASTMC** [29] was used for the detector simulations, including calorimeter energy smearing.

We give only a brief overview of exploratory results pertaining to the Standard Model Higgs boson with a mass in the range 110–125 GeV.

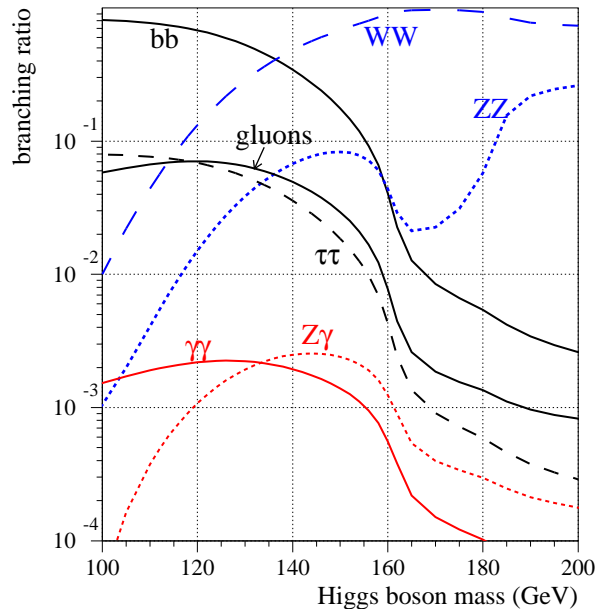


Figure 5: *The principal decay modes of the Higgs boson [45] in the mass range favoured by precision electroweak experiments.*

Mass

A special feature of the $\gamma\gamma$ collider is the sharp edge of the $\gamma\gamma$ luminosity function, as depicted in Fig. 2. The position of this edge can be controlled by changing the electron beam energy. As it sweeps across the threshold for Higgs production, the number of, e.g., $\bar{b}b$ events will increase dramatically. This phenomenon is already reflected in the sharpness of the excitation curves of Fig. 4. Since the position of this turn-on depends on the Higgs mass, a threshold scan offers the possibility to measure the Higgs mass kinematically, as developed in [30].

We have studied this possibility in the context of CLICHE [31], assuming that the Higgs mass is already known to within a GeV or so, from the Tevatron, the LHC or a e^+e^- linear collider. Considered as a function of the e^+e^- centre-of-mass energy, as shown in Fig. 4, there is a point of optimum sensitivity to the Higgs mass a few GeV below the peak of the cross section. The raw number of events at a single energy cannot be used to measure the mass, however, because the $\gamma\gamma$ partial width cannot be assumed known *a priori*. There is another point, though, close to the maximum of the cross section, at which there is no sensitivity to the Higgs mass, and with maximum sensitivity to $\Gamma_{\gamma\gamma}$, allowing the separation of these two quantities. These points are illustrated in Fig. 6. Furthermore, the background can be estimated using data obtained by running below the threshold. To estimate the sensitivity of the yields to m_H , we work with a simple observable based on the ratio of background-subtracted yields at peak and at threshold:

$$Y = \frac{N_{\text{peak}} - N_{\text{below}} \cdot r_p}{N_{\text{threshold}} - N_{\text{below}} \cdot r_t}$$

where N is the number of events in a mass window logged at the peak, on the threshold, and below threshold, and r_p and r_t are scale factors to relate the background data taken below threshold to the expectation at peak and at threshold. We have propagated statistical uncertainties, and, assuming one year of data on peak, half a year on threshold and another half below threshold, we find $\sigma_Y/Y = 0.088$. This translates into an error on the inferred Higgs mass of 100 MeV. A more refined treatment should improve this estimate somewhat. This estimate is obtained using the laser and beam energies proposed for CLIC 1 and the analysis results shown in Fig. 7. It is still necessary to investigate how sensitive the luminosity function is to the shape of the luminosity curve. It is not sensitive to the electron polarization precision.

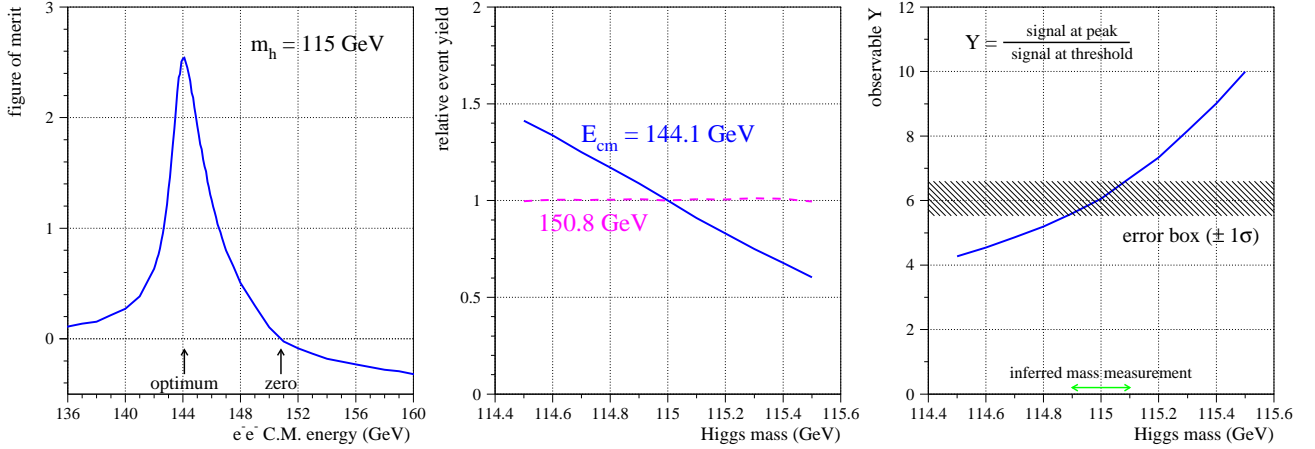


Figure 6: (a) A figure of merit quantifying the measurement error on the mass as a function of the e^+e^- centre-of-mass energy. The optimum and zero sensitivity points are marked. (b) Relative yield for a 115 GeV Higgs boson at the point of optimum sensitivity and zero sensitivity to m_H . (c) Behavior of the observable Y as a function of m_H , and the projected error.

$H \rightarrow \bar{b}b$:

Due to the large branching ratio for $H \rightarrow \bar{b}b$ decay for a Higgs mass ~ 115 GeV, this is the main channel for Higgs studies at CLICHE. This channel has received the most attention and the studies are already quite detailed [14, 32, 33]. Our analysis includes perturbative QCD backgrounds, including $\gamma\gamma \rightarrow \bar{b}b(g)$ and $\gamma\gamma \rightarrow \bar{c}c(g)$. The $\bar{q}q$ backgrounds are suppressed by choosing like polarizations for the colliding photons, but this suppression is not so strong when the final states contain additional gluons.

In this analysis we used the Durham jet algorithm and imposed a cut at $y = 0.02$ to define the two jets. The main cuts are: (1) only two-jet events are accepted, (we do not find any improvement if we include three-jet events as well), (2) $|\cos\theta| < 0.5$, which is 50% efficient, and (3) the two jets are required to be back-to-back. The last cut is very important for the background suppression, but at a significant cost in the signal. The efficiency of this cut is 85-90% for the 33% of events that do not contain neutrinos, but there is significant reduction in efficiency for the rest of the events. We assume here that there will be a 3.5% $c\bar{c}$ contamination

and that the b tagging is 70% efficient for double tagging [4]. The final reconstruction efficiency is expected to be 30%.

Recent photoproduction measurements of the b cross section at the highest energies at LEP are larger than predictions from NLO perturbative QCD calculations. L3 [34] and OPAL [35] report values for the cross section of $ee \rightarrow eeb\bar{b}X$ at $\sqrt{s} = 194$ GeV which are, respectively, 3σ and 2.5σ larger than predicted. Hadronic final states containing b quarks are identified by detecting leptons from their semi-leptonic decays. The effective $W_{\gamma\gamma}$ energy at which these measurements are made is considerably lower than the one at CLICHE, and it is therefore not clear that this will affect the signal-to-background ratio, in particular after all selection cuts made. This background can be controlled by measuring off the Higgs mass peak.

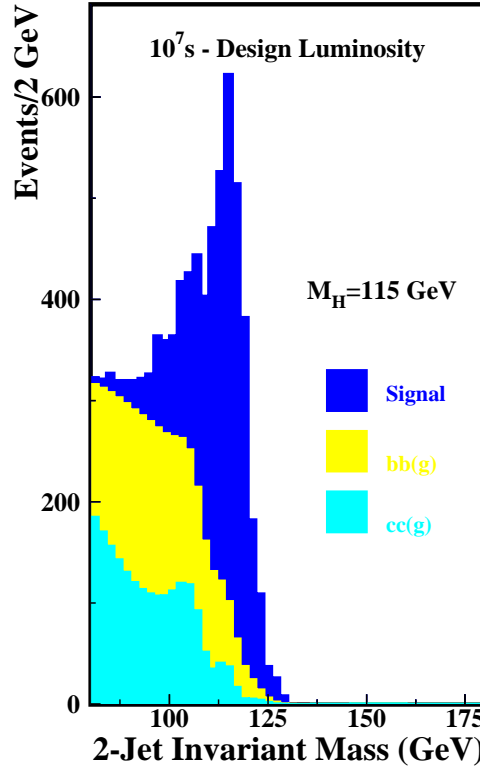


Figure 7: *Observability of the $H \rightarrow b\bar{b}$ decay mode for $m_H = 115$ GeV, with CLICHE running so that the peak $E_{CM}(\gamma\gamma) = 115$ GeV.*

The mass resolution is around 6 GeV with a jet energy resolution of $\sigma_E = 0.6 \times \sqrt{E}$. The distribution in the di-jet invariant mass, m_{jets} , for a $m_H = 115$ GeV Higgs found in this study with an integrated luminosity of 200 fb^{-1} is shown in Fig. 7. A clear signal peak can be seen above sharply falling backgrounds. Including the three bins nearest to $m_{jets} \sim 115$ GeV, we obtain 4952 signal events and 1100 background events. Thus, the signal-to-background ratio is expected to be 4.5 after all cuts.

A feature which is not taken into account in these studies is the pile-up of events from different bunch crossings. The bunch structure of CLIC leads to a bunch crossing every 0.67 nanoseconds. The detector components will generally not have the capability to time-stamp hits with this resolution and will provide information integrated over several bunch crossings. Hence an R&D program on the development of fast detectors will need to be pursued in the coming years (this is also the case for detectors at the NLC, where the separations between bunches are only a few nanoseconds). The components most likely to determine the total number of bunch crossings that will be integrated over, for the studies of interest here, will be the silicon pixel detectors, for which a time-stamping capability of 25 nsecs has been demonstrated for LHC experiments. It can be expected that this resolution will improve perhaps to 10 nsec or even 5 nsec within the next 10 years, based on present ideas that still need to be tested. Nevertheless, this means that of order 10 bunch crossings will contribute to measured events at CLICHE, which will affect the background shape of Fig. 7. This effect was not taken into account here, but initial studies have shown that it deteriorates the Higgs signal only slightly.

$H \rightarrow WW$:

Observation of this decay mode is extremely difficult at high-energy $\gamma\gamma$ colliders, because of the large cross section for W pair production. If the $\gamma\gamma$ centre-of-mass energy is below the W^+W^- threshold, however, the continuum production of W pairs is greatly reduced, allowing the observation of resonant production through a Higgs boson. The sharp peak in the $\gamma\gamma$ luminosity function seen in Fig. 2 plays a key role here. Figure 8(a) compares the cross sections for the continuum W pair production with the Higgs resonance curve. As shown, the cross sections for $\sigma(\gamma\gamma \rightarrow W^+W^-)$ and $\mathcal{B}r(h \rightarrow W^+W^-) \times \sigma(\gamma\gamma \rightarrow h)$ are comparable, if $E_{CM}(e^-e^-) = 150$ GeV for a $m_H = 115$ GeV. One significant difference between the two type of events is the energy distribution of the W^+W^- pairs, as illustrated in Figure 8(b).

Our study is concentrated on the hadronic decays of the W pairs, applying several kinematic cuts. One pair of jets must reconstruct to the W mass, while the other pair is required to saturate the remaining phase space. This cuts allows us not only to reduce the W^+W^- pairs to those with energy similar to those produced in Higgs events, but also to reject any possible $\gamma\gamma \rightarrow qq(g)$ background. There must be at least four jets in the event and the jet reconstruction efficiency is assumed to be 100%. In contrast to the $h \rightarrow b\bar{b}$ analysis, here we are imposing a $y = 0.003$ cut in the Durham algorithm used in the jet reconstruction. In addition, the transverse momentum is required to be smaller than 0.1. After these cuts we have a 29% reconstruction efficiency. A comparison of the signal and the background after cuts is given in Fig. 8(c), which corresponds to a signal-to-background ratio of 1.3, and the statistical precision in the signal rate measurement is expected to be 5%.

The other event topologies (two leptons and missing energy, or one lepton, missing energy and jets) remain to be studied. Techniques similar to those described in [36] may be used. We also believe that the decay $H \rightarrow ZZ, Z\gamma$ might be interesting, despite their relatively small branching ratios.

$H \rightarrow \gamma\gamma$:

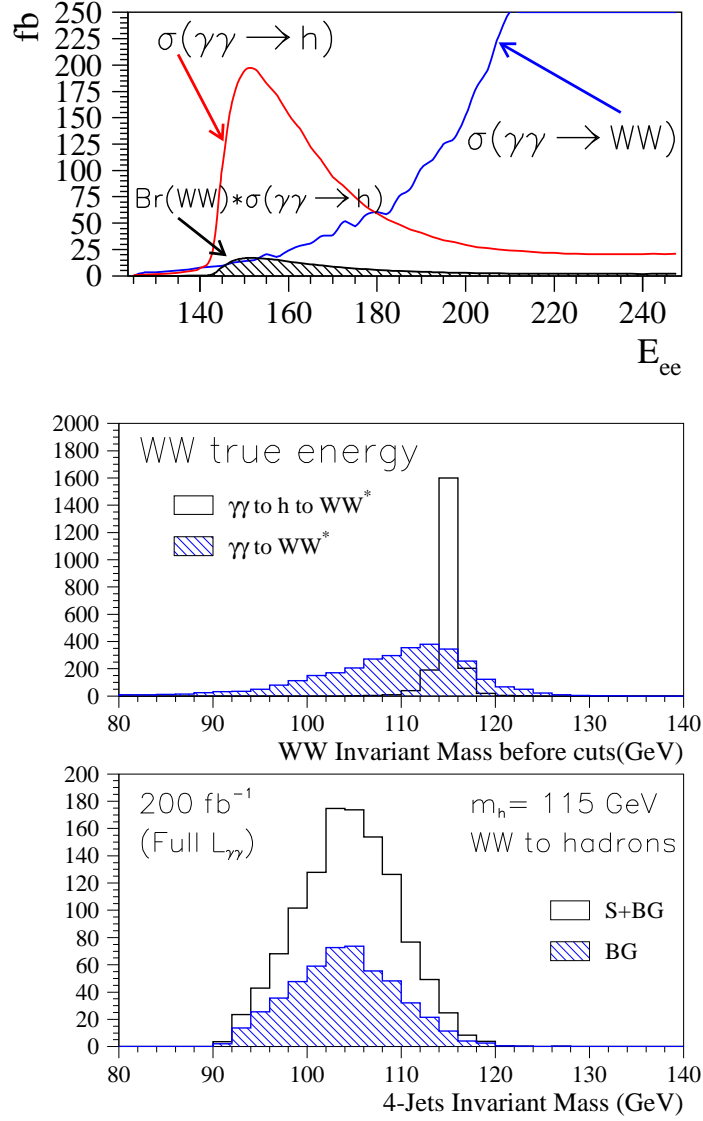


Figure 8: (a) Cross sections for $\gamma\gamma \rightarrow h$, $\gamma\gamma \rightarrow h \times Br(h \rightarrow WW)$ for $m_H = 115 \text{ GeV}$ and $\gamma\gamma \rightarrow WW$ production. (b) Comparison of the ideal invariant mass of the WW pairs from signal and background events. (c) Selection of the WW decay mode of the Higgs boson for $m_H = 115 \text{ GeV}$, running at $E_{CM}(\gamma\gamma) = 115 \text{ GeV}$ at CLICHE.

In almost any phenomenological context, the decay $H \rightarrow \gamma\gamma$ is a very rare one. However, the number of Higgs events is large at a $\gamma\gamma$ collider, so an interesting number of $H \rightarrow \gamma\gamma$ events would be produced. Furthermore, the backgrounds are expected to be quite small, below 2 fb [37], since there is no tree-level coupling of photons, and the box-mediated processes are peaked very sharply in the forward direction. A complete background study has not yet been made, but initial estimates indicate that a clear peak in the $\gamma\gamma$ mass distribution should be observable, and we assume here that the background error would be negligible.

The number of events produced in this channel is proportional to $\Gamma_{\gamma\gamma}^2/\Gamma_{\text{total}}$. The quadratic dependence is interesting, because if Γ_{total} could be measured elsewhere, a small error on $\Gamma_{\gamma\gamma}$ would be obtained. Similarly, if $\Gamma_{\gamma\gamma}$ is measured elsewhere, a small error Γ_{total} could be obtained. In Fig. 9, we can see that a 10% measurement of $\Gamma_{\gamma\gamma}^2/\Gamma_{\text{total}}$ can be made with less than a year of data taking.

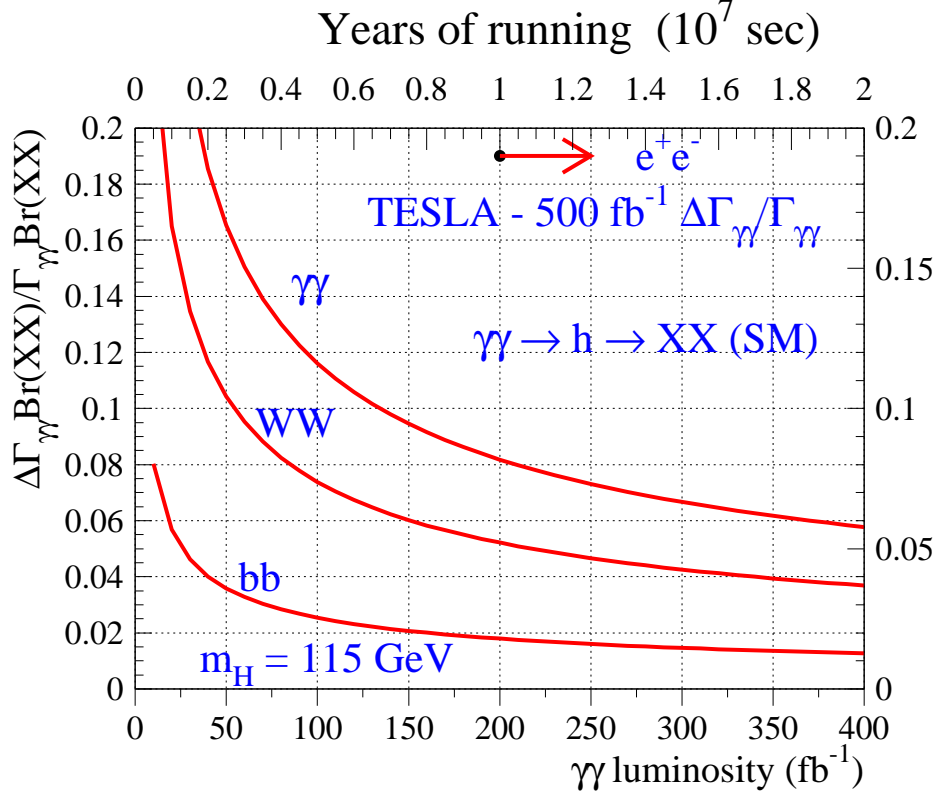


Figure 9: The expected precision in the $H \rightarrow \gamma\gamma$ decay width from direct measurements of $H \rightarrow \gamma\gamma$ for $m_H = 115$ GeV. The precision is less than in the equivalent measurement of $H \rightarrow WW, \bar{b}b$, but this observable is unique to a low-energy $\gamma\gamma$ collider like CLICHE.

The cleanliness of these events and good energy resolution in the electromagnetic calorimeter would allow for an independent measurement of the Higgs mass. Assuming that the calorimeter

energy scales can be sufficiently well calibrated, a resolution better than 100 MeV can be expected.

Other Channels:

A preliminary assessment of the $H \rightarrow \bar{c}c$ channel at a $\gamma\gamma$ collider is not very encouraging: relative to the $\bar{b}b$ mode, the $\bar{c}c$ signal is suppressed by factor of $(m_c/m_b)^2 \sim 1/10$, and the background is enhanced by a factor $(Q_c/Q_b)^4 = 16$. There is similar pessimism concerning the observability of $H \rightarrow gg$ and $H \rightarrow \tau^+\tau^-$.

Combining Channels:

A good measurement of the two-photon partial width, $\Gamma_{\gamma\gamma}$, is very important as it receives direct contributions from all charged massive particles, and there is no tree-level contribution. Since the Higgs production cross section is proportional to $\Gamma_{\gamma\gamma}$, the measurement of any yield provides information, in principle, on $\Gamma_{\gamma\gamma}$.

From the study of the channel $H \rightarrow \bar{b}b$ we estimate a precision of 2.0% on the quantity $\Gamma_{\gamma\gamma} \times \mathcal{B}r(H \rightarrow \bar{b}b)$. The branching ratio $\mathcal{B}r(H \rightarrow \bar{b}b)$ cannot be measured directly at a $\gamma\gamma$ collider, but there are methods for measuring it to about 1.5% at an e^+e^- linear collider [7, 3]. By combining the information from both colliders, $\Gamma_{\gamma\gamma}$ can be inferred to a precision of 2.2%, to be contrasted with a 19% measurement from 500 fb⁻¹ at TESLA (without the $\gamma\gamma$ option), for example.

As shown in Fig. 10, the $\Gamma_{\gamma\gamma}$ partial width in the MSSM can deviate a lot from the SM value; even for a fixed Higgs mass of 115 GeV, for example, a factor of two variation is possible. Note that this impacts the cross section and hence precision on the inferred value for $\Gamma_{\gamma\gamma}$. Nonetheless, it is clear that a precision of 2–4% would be very discriminating in the context of an unconstrained MSSM.

Alternatively, one could take the measurement of the yield in the $\bar{b}b$ channel at a $\gamma\gamma$ collider and combine it with measurements of the Higgs branching ratios to $\bar{b}b$ and $\gamma\gamma$ from an e^+e^- linear collider, and extract an indirect value for the total width:

$$\Gamma_{\text{total}} = \frac{\{\Gamma_{\gamma\gamma} \times \mathcal{B}r(H \rightarrow \bar{b}b)\}}{\{\mathcal{B}r(H \rightarrow \gamma\gamma)\} \times \{\mathcal{B}r(H \rightarrow \bar{b}b)\}}. \quad (2)$$

According to [38], the anticipated precision on $\mathcal{B}r(H \rightarrow \bar{b}b)$ and $\mathcal{B}r(H \rightarrow \gamma\gamma)$ are 2.4% and 19%, respectively. Combined with a precision of 2% on the numerator, this leads to a precision of about 20% for Γ_{total} .

A better measurement of Γ_{total} can be obtained by combining the 2% and 8% measurements of $H \rightarrow \bar{b}b$ and $H \rightarrow \gamma\gamma$ with the expected 1.5% measurement of the $\mathcal{B}r(H \rightarrow \bar{b}b)$ from the e^+e^- linear collider [3, 7]. In this case a 9% measurement of the Γ_{total} can be inferred, compared to the 4–6% measurement from 500 fb⁻¹ at TESLA [3].

CP

Table 3: *The statistical errors on selected decay modes of a 115 GeV Higgs boson in the Standard Model. The $\gamma\gamma \rightarrow h$ cross section for the full (peak) $\mathcal{L}_{\gamma\gamma}$ given in Table 2 is 112 (624) fb. The expected yield for 200 (36) fb $^{-1}$ is 22,400 Higgs particles.*

decay mode	raw events/year	S/B	ϵ_{sel}	$\mathcal{B}r$	$\Delta\Gamma_{\gamma\gamma}\mathcal{B}r/\Gamma_{\gamma\gamma}\mathcal{B}r$
$b\bar{b}$	16509	4.5	0.30	73.7%	2%
W^+W^-	1971	1.3	0.29	8.8%	5%
$\gamma\gamma$	45	—	0.70	0.2%	8%

A measurement that might be unique for $\gamma\gamma$ collider experiments like CLICHE could be that of the CP properties of the $H \rightarrow \gamma\gamma$ vertex [39], which can be measured by colliding photons with orthogonal linear polarizations, which define initial states of definite CP. In the Standard Model, the $H \rightarrow \gamma\gamma$ vertex has only a CP-even part, but in extended models, such as supersymmetry, there may also be a CP-odd part, which could provide an interesting window on the mystery of CP violation. The CP properties of the $H \rightarrow \gamma\gamma$ vertex are in principle distinct from those of other Higgs vertices, and hence have independent interest. This measurement would require higher-energy electrons and producing the photons using lasers of longer wavelength in order to reduce the interference and obtain a state with CP better defined [40, 14].

Another window on the CP nature of the Higgs boson is provided by angular distributions in the $H \rightarrow W^+W^-$ channel [41]. This channel is useful because information can be obtained even in the absence of linearly-polarized photon beams. A rough estimate gives $\delta A/A \sim 5\%$ or better from the measurements that could be made at CLICHE.

Summary:

We have briefly discussed measurement possibilities in the $\bar{b}b$, W^+W^- and $\gamma\gamma$ channels. The observabilities and statistical errors of the products $\sigma(\gamma\gamma \rightarrow H) \times \mathcal{B}r(H \rightarrow X)$ for each of these decay modes are summarized in Table 3. Preliminary studies indicate that the systematic errors, *e.g.*, those due to the luminosity and polarization uncertainties, could be controlled to the same level. Thus it seems possible to measure $\sigma(\gamma\gamma \rightarrow H \rightarrow \bar{b}b, WW, \gamma\gamma)$ with overall precisions of 2, 5, 8%, respectively (see Fig. 9).

In addition, the Higgs mass can be measured three ways (fitting the peaks in the $\bar{b}b$ and $\gamma\gamma$ mass distributions, and by the threshold method), and the partial width $\Gamma_{\gamma\gamma}$ can be extracted on the basis of a measurement of $\mathcal{B}r(H \rightarrow \bar{b}b)$ from an e^+e^- collider to very good accuracy, not matched by any other method. Finally, possible CP asymmetries could be measured with a precision of about 5%.

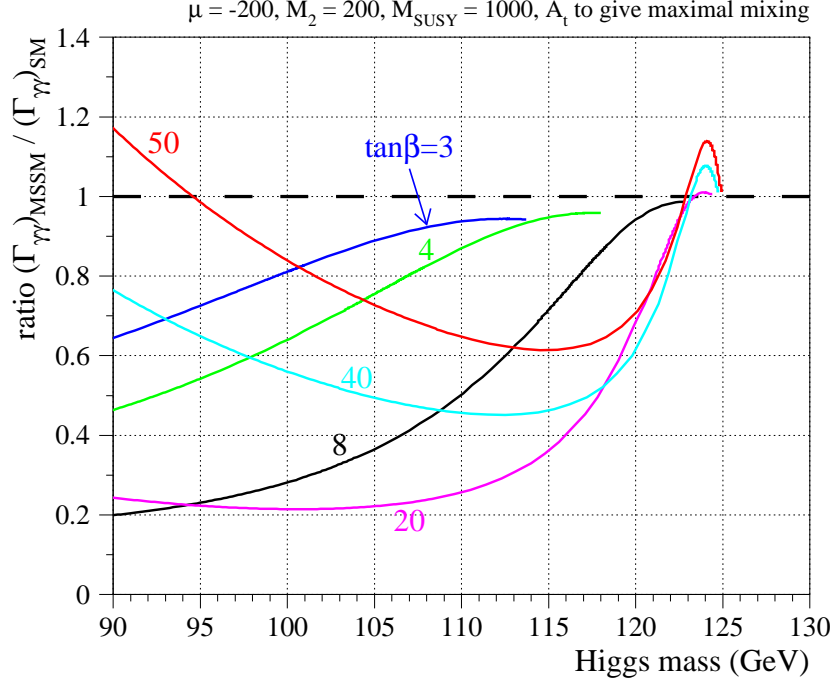


Figure 10: The ratio of the partial width $\Gamma_{\gamma\gamma}$ in the MSSM to that in the SM [45]. The ‘maximal mixing’ [44] scenario has been chosen for this illustrative plot; this scenario tends to give the largest Higgs masses for a given $\tan\beta$ and M_A . These curves do not necessarily map out the largest possible variation in this ratio, nor have they been constrained by negative searches for Higgs bosons. The ratio of cross sections follows the same curves.

3.1.2 Complementarity with other Machines

Each of the combinations $\Gamma(H \rightarrow \gamma\gamma) \times \mathcal{B}r(H \rightarrow \bar{b}b, WW, \gamma\gamma)$ measurable at CLICHE is distinct from the quantities observable previously at the Tevatron: $\Gamma(H \rightarrow W^+W^-) \times \mathcal{B}r(H \rightarrow \bar{b}b)$, and the LHC: $\Gamma(H \rightarrow gg) \times \mathcal{B}r(H \rightarrow \gamma\gamma)$ and $\Gamma(H \rightarrow \bar{t}t) \times \mathcal{B}r(H \rightarrow \bar{b}b)$. It is estimated that the Tevatron observable could be measured with a precision of 20% and the LHC observables with precisions $\sim 7, 10\%$, respectively. The CLICHE measurement of $\Gamma(H \rightarrow \gamma\gamma) \times \mathcal{B}r(H \rightarrow \bar{b}b)$ would therefore be complementary to, and of higher accuracy than, these previous measurements, whilst the other CLICHE measurements would also be competitive.

At an e^+e^- collider, the Higgs bosons to be used in the the branching-ratio measurements are observed in the Higgsstrahlung production process $e^+e^- \rightarrow H + Z$, with the $Z \rightarrow \ell^+\ell^-$ fully reconstructed. A data set of 500 fb^{-1} with $E_{CM}(e^+e^-) = 350 \text{ GeV}$ (500 GeV), corresponding to one to three years of TESLA (NLC), provides a sample of 2200 to 3500 Higgs particles produced in the $H + (Z \rightarrow \ell^+\ell^-)$ channel, for $m_H = 120$ to 200 GeV. The raw number of Higgs particles to be produced in one of these machines is around 20,000. An e^+e^- collider with energy $\sim 500 \text{ GeV}$ would be able to measure with high precision $\Gamma(H \rightarrow ZZ)$ and all the dominant

decay branching ratios $H \rightarrow \bar{b}b, \bar{c}c, gg, \tau^+\tau^-$ shown in Fig. 5. Moreover, such an e^+e^- collider could also be configured as a $\gamma\gamma$ collider, if it is equipped with a laser backscattering facility. This possibility is envisaged in the current designs of the JLC [25], NLC [7] and TESLA[8], but may not be scheduled for the initial phases of these machines.

At CLICHE, one could have 150 fb^{-1} in a year with $E_{CM}(e^-e^-) = 150 \text{ GeV}$ and a $\gamma\gamma$ centre-of-mass energy peaked at 115 GeV. We recall that a 115 GeV Higgs would be produced as an s -channel resonance, and that the event yield is estimated to be around 22,000 per year. Similar yields could be expected for $m_H \leq 125 \text{ GeV}$ (see Fig. 4(b)), if the extra energy was made available.

3.1.3 Discriminating between Higgs Models using CLICHE Measurements

Since the $H \rightarrow \gamma\gamma$ vertex is due to loop diagrams, it is sensitive to physics beyond the direct physics reach of CLICHE. For example, a 3% measurement of $\Gamma(H \rightarrow \gamma\gamma)$ would provide indirectly a 6% measurement of $\Gamma(H \rightarrow t\bar{t})$, in the absence of new physics [42]. However, supersymmetry is a prime example of possible new physics that could influence the $H \rightarrow \gamma\gamma$ vertex, as seen in Fig. 10.

As an example how the precision achievable with CLICHE could help distinguish between models of Higgs bosons, in the following we compare Higgs production in $\gamma\gamma$ collisions in the Standard Model and its minimal supersymmetric extension, the MSSM. We do this by calculating the product of the production cross section and branching ratio for the lightest MSSM Higgs boson, h , normalized to the corresponding Standard Model value, with M_H set to the mass of the lightest MSSM Higgs, M_h :

$$R_{b,W,\gamma} := \frac{[\Gamma(\gamma\gamma \rightarrow h) \times \mathcal{B}r(h \rightarrow \bar{b}b, WW^*, \gamma\gamma)]_{\text{MSSM}}}{[\Gamma(\gamma\gamma \rightarrow H) \times \mathcal{B}r(H \rightarrow \bar{b}b, WW^*, \gamma\gamma)]_{\text{SM}}} . \quad (3)$$

Regions of the MSSM parameter space with strong deviations from the Standard Model are identified in the following. Strong suppression of these ratios could occur in problematic corners of the MSSM parameter space, where a specific decay channel or even MSSM Higgs production itself is inaccessible. The evaluation of the Higgs boson sector has been performed with the codes **FeynHiggs** [43], based on [44], and **Hdecay** [45].

In Figs. 11-13, the unconstrained MSSM is analyzed in three benchmark scenarios [46], originally proposed in connection with Higgs searches at LEP. The ‘ m_h^{max} ’ scenario maximizes the m_H value for a given $M_A, \tan\beta$ combination at fixed M_{SUSY} and m_t . The ‘no-mixing’ scenario has the same parameters as the m_h^{max} scenario, but no scalar top mixing. Contrary to [46], we have set $M_{SUSY} = 1500 \text{ GeV}$ and $m_{gl} = 1000 \text{ GeV}$ so as to increase the m_h values. In the last scenario, the value of μ is chosen to be large: $\mu = 1 \text{ TeV}$. Contrary to [46], we have again set $M_{SUSY} = 1000 \text{ GeV}$ so as to increase the m_h values. The limits of LEP Higgs searches have been applied in these figures, using an updated version of the results as presented in [47]. However, the ‘no-mixing’ and ‘large μ ’ scenarios have $m_h \lesssim 120 \text{ GeV}$ for the shown parameter space, whereas the m_h^{max} scenario results in $m_h \gtrsim 125 \text{ GeV}$ for large parts of the

parameter space, which is at the limit of the reach of CLICHE. An analysis of similar scenarios for a TeV-class e^+e^- linear collider can be found in [48].

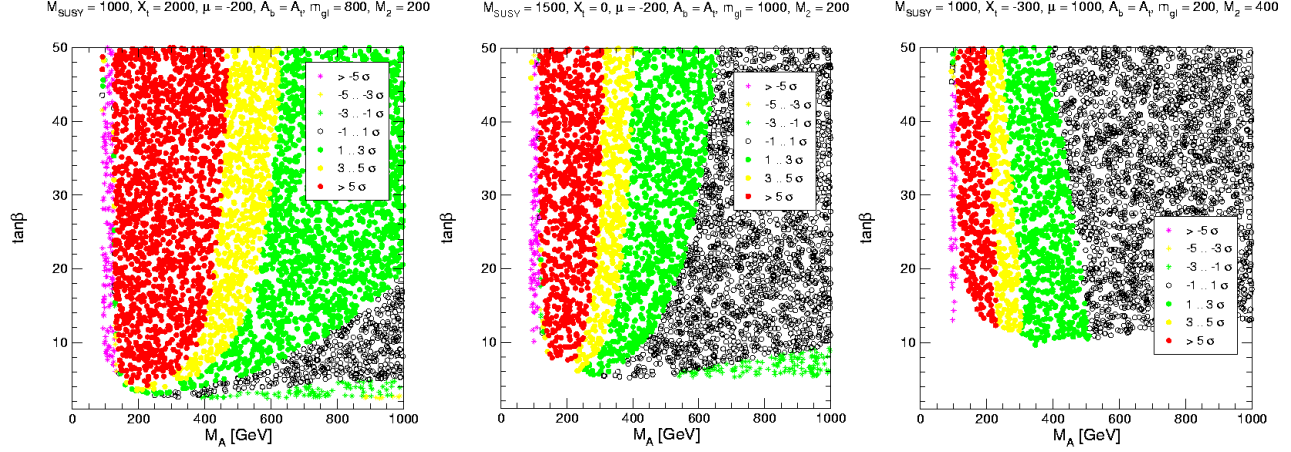


Figure 11: The ratio R_b is shown in the $M_A, \tan\beta$ plane for the three benchmark scenarios described in the text. The observable deviation from the Standard Model is indicated for a 2% experimental precision in R_b .

In Fig. 11, R_b is shown in the $M_A, \tan\beta$ plane. As expected, due to the enhanced $hb\bar{b}$ coupling, R_b is enhanced in most part of the parameter space in all three benchmark scenarios. Suppression only occurs for very small values of M_A : $M_A \lesssim 130$ GeV or small $\tan\beta$, $\tan\beta \lesssim 5$. Deviations from the Standard Model at the 3-5 σ level can be observed up to $M_A \lesssim 300 - 500$ GeV, depending on the scenario. We note deviations from the Standard Model at the 1 σ level in nearly the whole plane in the m_h^{\max} scenario and up to $M_A \lesssim 500 - 600$ GeV in the other scenarios. These sensitivities are in the same ballpark as for a linear e^+e^- collider [48]. Thus, a $\gamma\gamma$ collider could offer a complementary method of distinguishing the MSSM from the SM in the Higgs sector.

Figs. 12 and 13 show R_W and R_γ , respectively, for the three benchmark scenarios. As one would expect from the enhancement in R_b , these two channels are usually suppressed. There are cases in which R_W and R_γ are strongly enhanced (by a factor three or four), though these cases are not typical. Extremely strong suppressions can occur in all scenarios for $M_A \lesssim 300$ GeV, rendering these channels more difficult to observe. Deviations from the Standard Model at the 1 σ level or better can be found up to $M_A \lesssim 600 - 1000$ GeV. Thus, these channels could also offer interesting opportunities to find deviations from the Standard Model over a wide range of MSSM parameter space.

Contrary to the unconstrained MSSM, where analyses have to be restricted to certain benchmark scenarios, the full parameter space can be explored in the CMSSM, where the soft supersymmetry-breaking scalar masses m_0 and fermion masses $m_{1/2}$ are assumed to be universal at some input unification scale. Here we restrict ourselves to $A_0 = 0$ and positive μ . An exhaustive study can be found in [49], and a similar study for the Tevatron and the LHC is

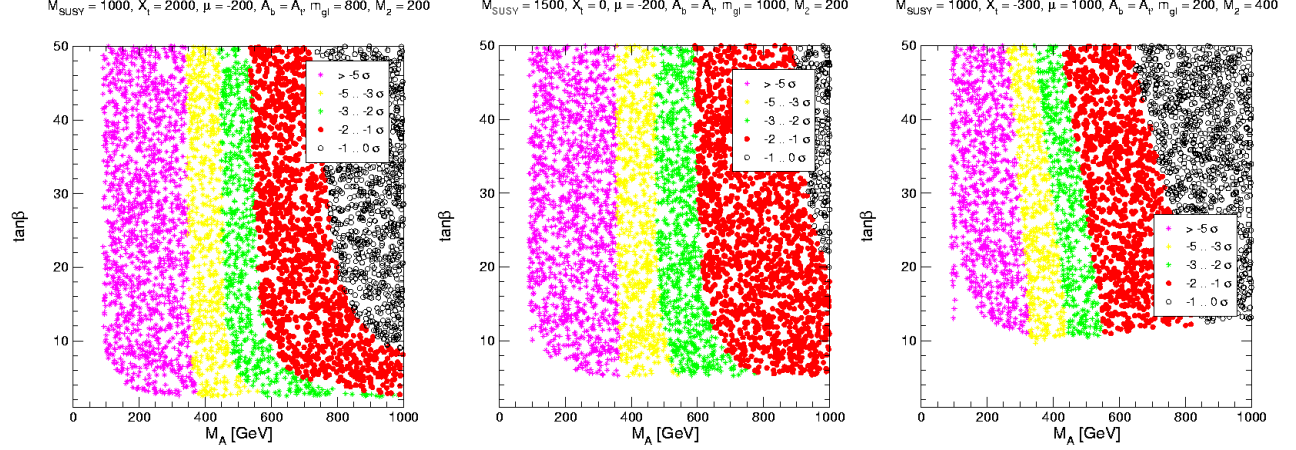


Figure 12: The ratio R_W is shown in the $M_A, \tan\beta$ plane for the three benchmark scenarios described in the text. The observable deviation from the SM is indicated for a 5% experimental precision in R_W .

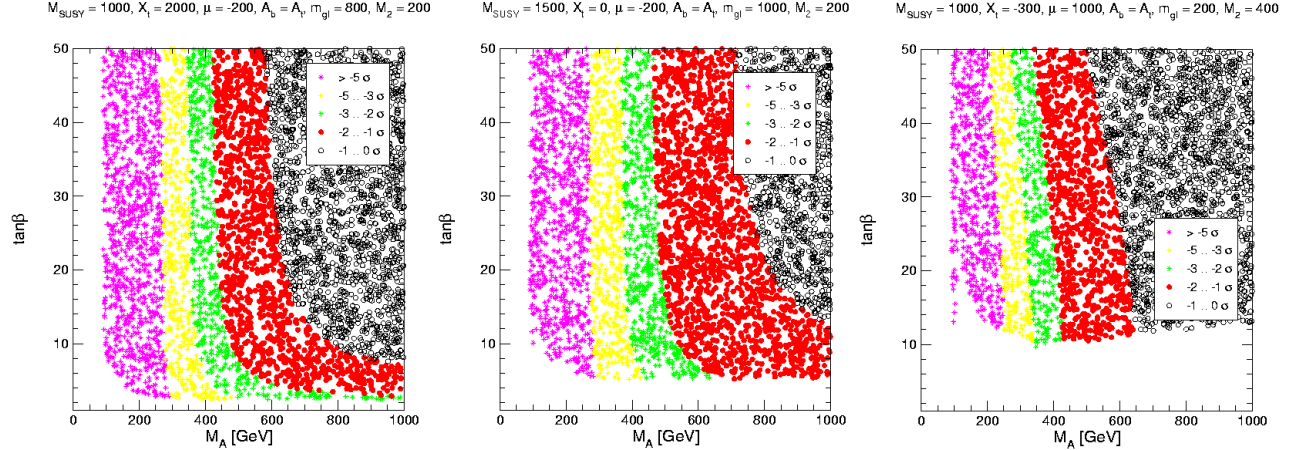


Figure 13: The ratio R_γ is shown in the $M_A, \tan\beta$ plane for the three benchmark scenarios described in the text. The observable deviation from the SM is indicated for a 8% experimental precision in R_γ .

given in [50].

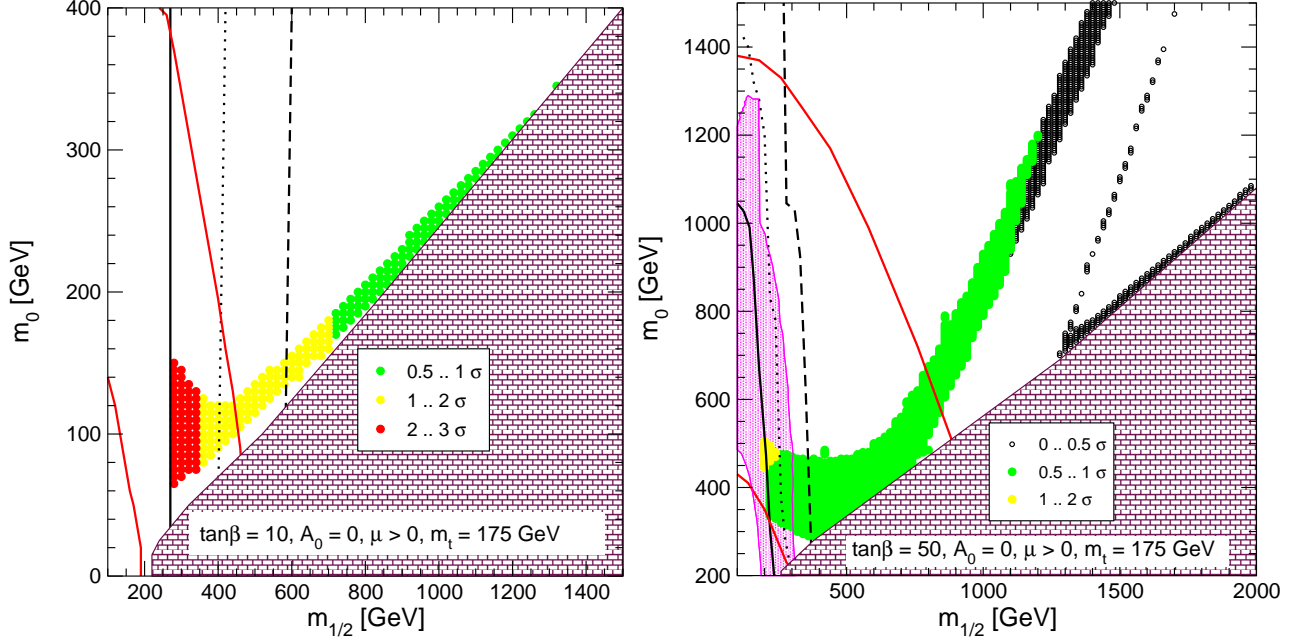


Figure 14: the ratio R_b is shown in the $m_0, m_{1/2}$ plane for $\tan\beta = 10, 50$ and $\mu > 0$, $A_0 = 0$. The diagonal (red) solid lines are the $\pm 2\sigma$ contours for $g_\mu - 2$. The near-vertical solid, dotted and dashed (black) lines are the $m_H = 113, 115, 117$ GeV contours. The light shaded (pink) regions are excluded by $b \rightarrow s\gamma$. The (brown) bricked regions are excluded since in these regions the lightest sparticle is the charged $\tilde{\tau}_1$. The observable deviation from the Standard Model is indicated for a 2% experimental precision of R_b .

The ratios $R_{b,W,\gamma}$ are shown in Figs. 14-16 in the $m_{1/2}, m_0$ plane for $\tan\beta = 10, 50$, $\mu > 0$ and $A_0 = 0$. Only the parameter space that gives acceptable values for a CMSSM explanation of cold dark matter, $0.1 \leq \Omega_{CDM} h^2 \leq 0.3$, is analyzed: see [51] for details. Correspondingly, the regions with a $\tilde{\tau}$ LSP are marked as excluded. In addition, the regions disfavored by measurements of $\mathcal{B}r(b \rightarrow s\gamma)$ [52] are indicated, as are the regions preferred by the recent $g_\mu - 2$ measurement [53].

As in the unconstrained MSSM, R_b is enhanced in the CMSSM, whereas R_W and R_γ are suppressed. Larger deviations are observed for lower values of $m_{1/2}$ and m_0 , which are also preferred by the $g_\mu - 2$ measurement. For $\tan\beta = 10$, up to 3σ could be observable, whereas for $\tan\beta = 50$ the maximal deviation of the MSSM from the SM could be 2σ . Similar values would be obtainable at a linear e^+e^- collider [49]. Therefore, since it uses a different production process, a $\gamma\gamma$ collider could provide additional complementary information to the results obtainable at a linear e^+e^- collider.

Generally, it is expected that supersymmetry, if it exists, will be discovered at the LHC via the production and observation of sparticles. However one can construct also so-called

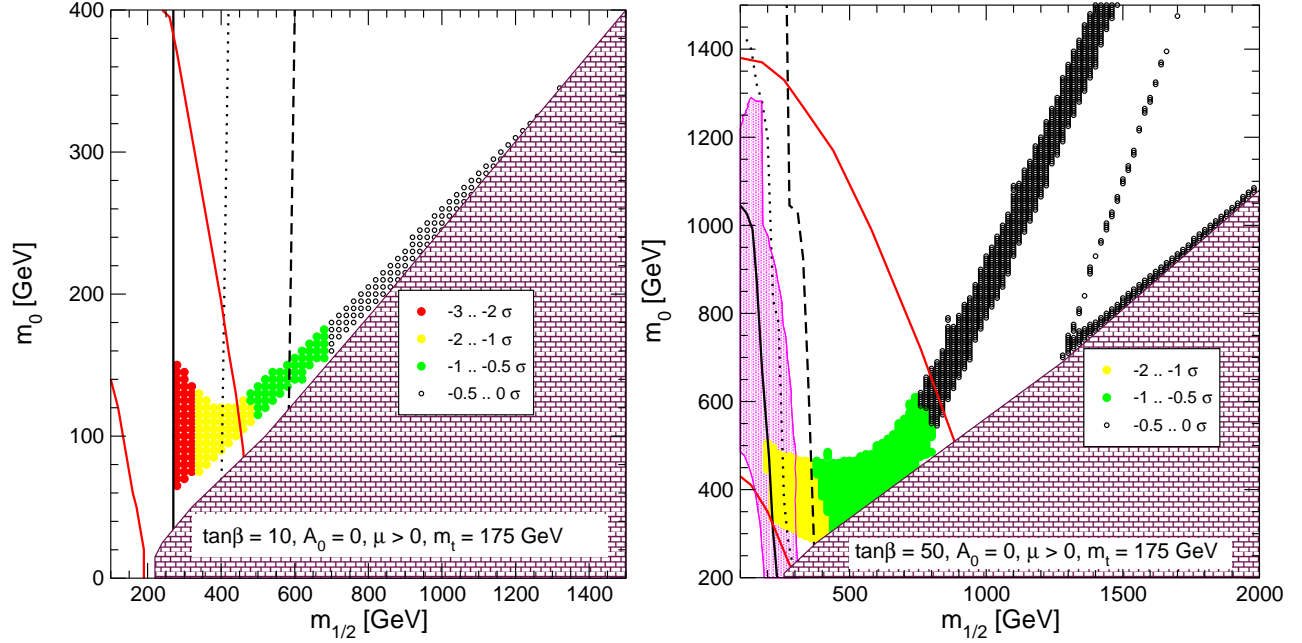


Figure 15: The ratio R_W is shown in the $m_0, m_{1/2}$ plane for $\tan\beta = 10, 50$ and $\mu > 0$, $A_0 = 0$. The diagonal (red) solid lines are the $\pm 2\sigma$ contours for $g_\mu - 2$. The near-vertical solid, dotted and dashed (black) lines are the $m_H = 113, 115, 117$ GeV contours. The light shaded (pink) regions are excluded by $b \rightarrow s\gamma$. The (brown) bricked regions are excluded since in these regions the lightest sparticle is the charged $\tilde{\tau}_1$. The observable deviation from the Standard Model is indicated for a 5% experimental precision of R_W .

Standard-Model-like scenarios where only one light Higgs boson will be within the reach of the LHC and future linear e^+e^- colliders, and its measured couplings to quarks, leptons and gauge bosons will be in agreement with their SM expectation within experimental errors.

Such scenarios can be constructed in MSSM and in more general two-Higgs-Doublet Models (2HDM), as demonstrated in [54]. In the latter study, the authors took the CP-conserving 2HDM in its model II implementation, where one doublet of fundamental scalar fields couples to the u quarks and the other to the d quarks and charged leptons. The experimental accuracies with which couplings are expected to be measured at a 500 GeV e^+e^- linear collider are taken into account in the definition of a parameter space in the 2HDM where it would be indistinguishable from the Standard Model. Hence, the Higgs mimics all the Standard Model properties one can expect to be measured using LHC and linear collider data.

Measuring the partial width of the Higgs to photons can distinguish between such scenarios. Due to the contribution to the $H\gamma\gamma$ coupling of all charged particles, including the very heavy ones, the ratio of the Higgs boson width in the 2HDM to the one in the Standard Model can differ significantly from unity. An example is shown in Fig. 17 for a 2HDM solution which satisfies all the Standard-Model-like criteria. The possible deviation from the Standard Model

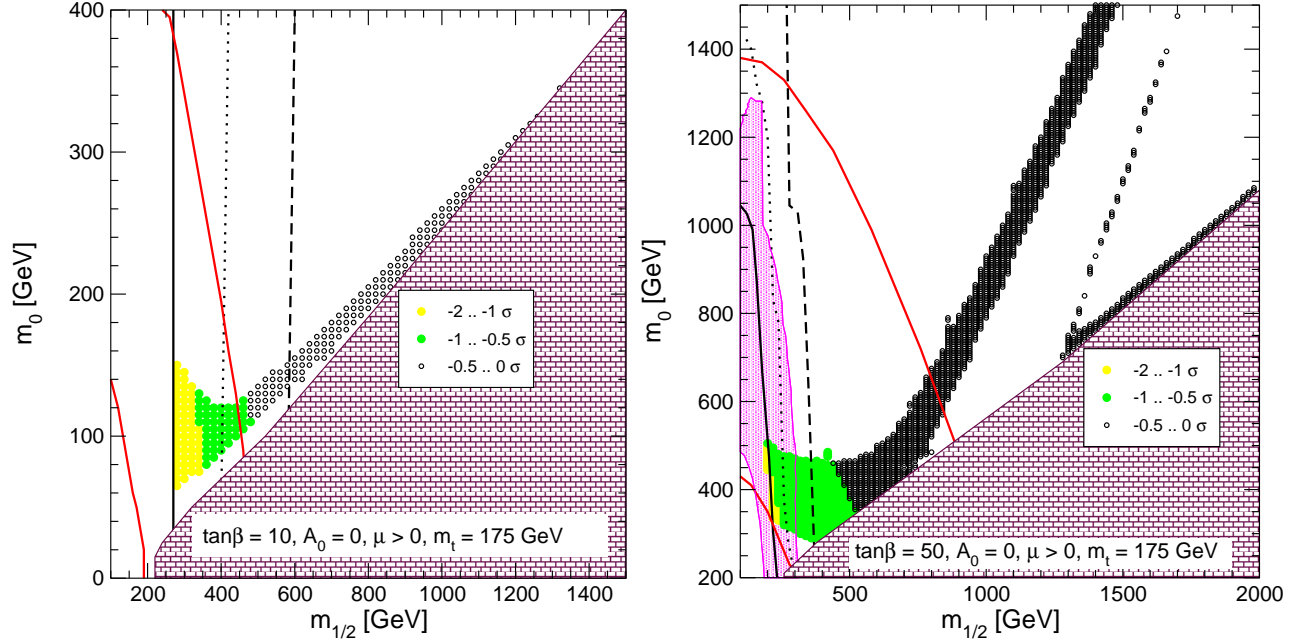


Figure 16: The ratio R_γ is shown in the $m_0 - m_{1/2}$ plane for $\tan \beta = 10, 50$ and $\mu > 0$, $A_0 = 0$. The diagonal (red) solid lines are the $\pm 2\sigma$ contours for $g_\mu - 2$. The near-vertical solid, dotted and dashed (black) lines are the $m_H = 113, 115, 117$ GeV contours. The light shaded (pink) regions are excluded by $b \rightarrow s\gamma$. The (brown) bricked regions are excluded since in these regions the lightest sparticle is the charged $\tilde{\tau}_1$. The observable deviation from the Standard Model is indicated for a 8% experimental precision of R_γ .

for $m_H \sim 120$ GeV is considerably larger than the error in the $\gamma\gamma \rightarrow H \rightarrow \bar{b}b$ signal expected from CLICHE. This stresses the importance of accurate measurements of the two photon width of the Higgs, and the correspondingly unique role of a precision photon collider in disentangling physics beyond the Standard Model.

3.2 QCD Physics in $\gamma\gamma$ Collisions

QCD aspects of $\gamma\gamma$ physics have been studied at e^+e^- colliders over the last 20 years. At LEP, $\gamma\gamma$ collisions with $\sqrt{s}(\gamma\gamma)$ up to 140 GeV have been studied. Up to now, the photons have been produced via bremsstrahlung [55] from the electron and positron beams, leading to soft energy spectra with only limited statistics at high $\sqrt{s}(\gamma\gamma)$, whereas CLICHE will produce $\gamma\gamma$ collisions in the high-energy part of the spectrum. A plethora of QCD physics topics in two-photon interactions can be addressed with a $\gamma\gamma$ collider, as recently discussed in [8]. Furthermore, good knowledge and understanding of two-photon processes will be essential for controlling physics background contributions to other processes and machine backgrounds at TeV and multi-TeV linear e^+e^- colliders.

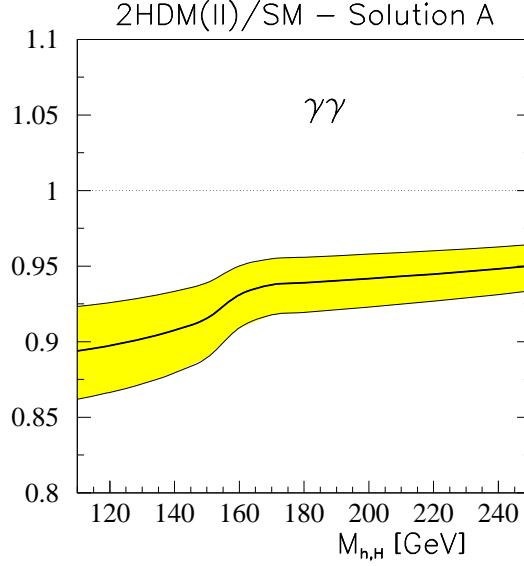


Figure 17: Ratios of the Higgs boson $\gamma\gamma$ -decay width in the 2HDM and the Standard Model as functions of $m_{h,H}$, assuming that all basic couplings are indistinguishable from those in the Standard Model [54].

A key issue is the total $\gamma\gamma$ cross section, which is not yet understood from first principles. Present data show a rise in $\gamma\gamma$ collisions that may be faster than that in pp , but the experimental errors are still large. At a $\gamma\gamma$ collider such as CLICHE, the photon beam energy can be tuned with a spread of less than 10%, so that measurements of $\sigma_{tot}(\gamma\gamma)$ can be made at a number of ‘fixed’ energy values. The absolute precision with which these cross-sections can be measured ranges from 5% to 10%, according to studies made for the $\gamma\gamma$ option of TESLA [8].

Quantum fluctuations of the photon into quarks or bound states lead to the so-called hadronic structure of the photon. The absolute magnitude of the photon hadronic structure function is asymptotically determined by the strong coupling constant [56]. The classical way to study the structure of the photon is via deep inelastic electron-photon scattering, i.e., two-photon interactions with one quasi-real (virtuality $Q^2 \sim 0$) and one virtual ($Q^2 > \text{few GeV}^2$) photon, which can be achieved by switching off one of the laser beams. Making the reasonable assumption that the scattered electron can be detected down to 25 mrad, measurements can be made in the region $5.6 \cdot 10^{-4} < x < 0.56$, where x is the fraction of the photon momentum carried by a constituent parton, and $10 < Q^2 < 8 \cdot 10^3 \text{ GeV}^2$.

Although $e\gamma$ scattering allows one to measure the quark distributions inside the photon, it constrains only weakly the gluon distribution, via the QCD evolution of the structure functions. Direct information on the gluon in the photon can, however, be obtained from measurements of jets [57], open charm [58] and J/ψ [59] production in $\gamma\gamma$ interactions at an $e\gamma$ and $\gamma\gamma$ collider. Values of x down to a few $\times 10^{-3}$ can be reached with charm and di-jet measurements [57, 58],

a region where predicted gluon distributions typically differ by a factor of two or more.

We also recall the deviation [34, 35] from the NLO QCD predictions of the $b\bar{b}$ cross section in $\gamma\gamma$ collisions measured at LEP, which was mentioned earlier. It is unlikely that this matter will be settled by further analysis of the LEP data, and CLICHE could revisit the study of the $b\bar{b}$ cross section. It will allow accurate measurements as functions of $W_{\gamma\gamma}$ and other kinematical variables to identify the origin of the putative anomaly.

A linear collider also provides circularly-polarized photon beams, which offer a unique opportunity to study the polarized parton distributions of the photon, for which no experimental data are available so far. Information on the spin structure of the photon can be obtained from inclusive polarized deep-inelastic $e\gamma$ measurements and from jet and charm measurements [60, 61] in polarized $\gamma\gamma$ scattering. Measurements of g_1 , particularly at low x , are very important for studies of the high-energy QCD limit, where signs of the BFKL regime [62] may appear.

Other dedicated measurements have been proposed for detecting and studying the large $\ln 1/x$ logarithm resummation effects in QCD. One example is vector meson production, e.g., $\gamma\gamma \rightarrow J/\psi J/\psi$ or (at large t) $\gamma\gamma \rightarrow \rho\rho$, where the hard scale in the process is given by the J/ψ mass or the momentum transfer t . The J/ψ can be detected via its decay into leptons, and separated from the background via its peak in the $\ell^+\ell^-$ invariant mass. Other processes that are strongly sensitive to BFKL effects include $e\gamma$ scattering with associated jet production [63], and $e^+e^- \rightarrow e^+e^-\gamma X$ and $\gamma\gamma \rightarrow \gamma X$ [64].

3.3 $e^-\gamma$ Physics

The option of $e^-\gamma$ collisions is available along with $\gamma\gamma$ and e^-e^- collisions, because the e^- conversion efficiency is, by design, less than 100%. The expected luminosity spectra for different spin states provided by the CLICHE design described previously are shown in Fig. 18. Moreover, if one wanted 50% higher $e^-\gamma$ luminosity at the peak, one could switch off one of the laser backscattering systems at cost of a factor of two in the total $e^-\gamma$ luminosity. Among the reactions of potential interest, we mention $e^-\gamma \rightarrow \nu W^-$. As seen in Fig. 19, the cross section for this process rises rapidly with $E_{CM}(e^-e^-)$ in the range accessible to CLICHE. This reaction could in principle be used to measure m_W and/or Γ_W . The result of one exploratory study is shown in Fig. 20. It shows the accuracy attainable in a measurement of Γ_W as a function of the available integrated $e^-\gamma$ luminosity. We see that a CLICHE measurement could become competitive for a luminosity of 50 fb^{-1} or more.

4 Outlook

The technology to build a machine like CLIC is under active development, but is not available today. Important progress in establishing the two-beam acceleration technique, as a novel

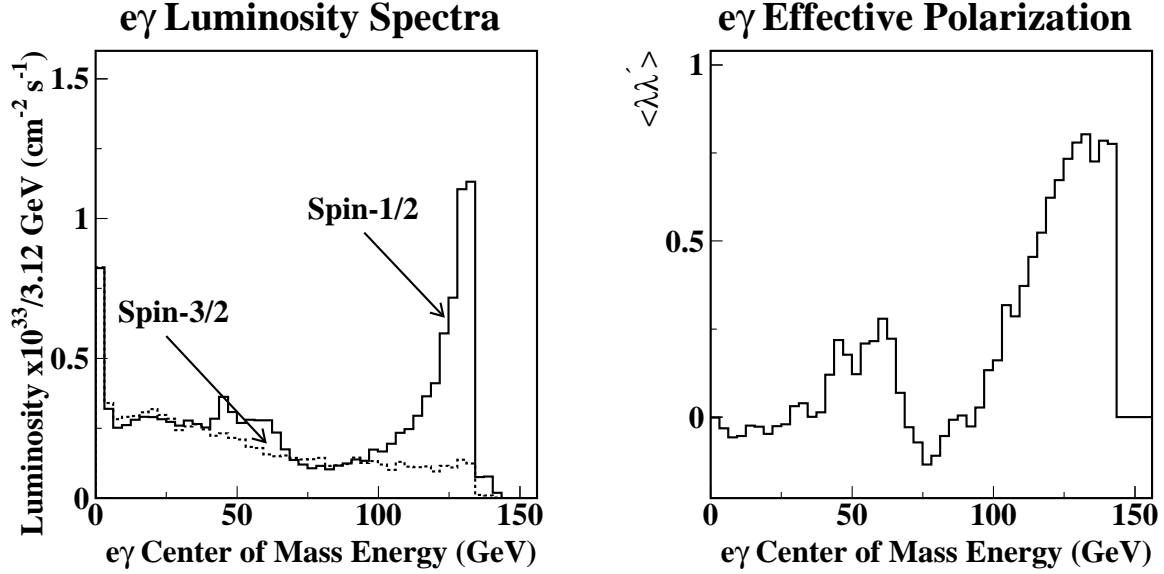


Figure 18: *Luminosity spectra and polarization for different spin states as functions of $E_{CM}(e^-\gamma)$, assuming the CLIC 1 parameters for 75 GeV electrons obtained with DIMAD [20] and CAIN [26] for $\mathcal{L}_{ee} = 4.8 \times 10^{34} \text{cm}^{-2} \text{s}^{-1}$.*

method to obtain large gradients, has been made over the last 5 years with the CLIC Test Facilities 1 and 2. Presently, a new test facility is being prepared to demonstrate the principle of all ingredients needed to build up the required drive beam. The final results of this test facility are expected by the end of 2006, and, if successful, this could initiate the preparation of a Technical Design Report for a machine based on CLIC technology. As mentioned in the Introduction to this paper, the next technological step towards a multi-TeV collider could be the construction and operation of one (or, as we suggest, two) full CLIC module(s), providing acceleration by about 70 GeV. By the time one would have to define the physics objectives of such a CLIC 1 stage, it will be clear from the Tevatron and LHC if the Higgs exists and is within the mass reach of CLICHE.

In this scenario, CLICHE could be contemporary with the operation of a TeV-class e^+e^- linear collider such as TESLA, NLC or JLC. The complementary information on the Higgs boson provided by CLICHE could be very valuable and help to distinguish among models.

All the above linear collider proposals consider a $\gamma\gamma$ collider as an option that could be added to their baseline programmes. The physics programme of a higher- E_{CM} $\gamma\gamma$ collider has been amply documented [7, 8]. Here we just recall that such a machine could provide a unique window on the heavier neutral Higgs bosons H, A expected in the MSSM and 2HDM [13, 14, 54], and would offer bright prospects for unravelling their CP properties. The high-energy physics programme for an e^+e^- collider is by itself so rich that one can expect any photon collider option to start only several years of the start-up of the facility. The experience on photon colliders

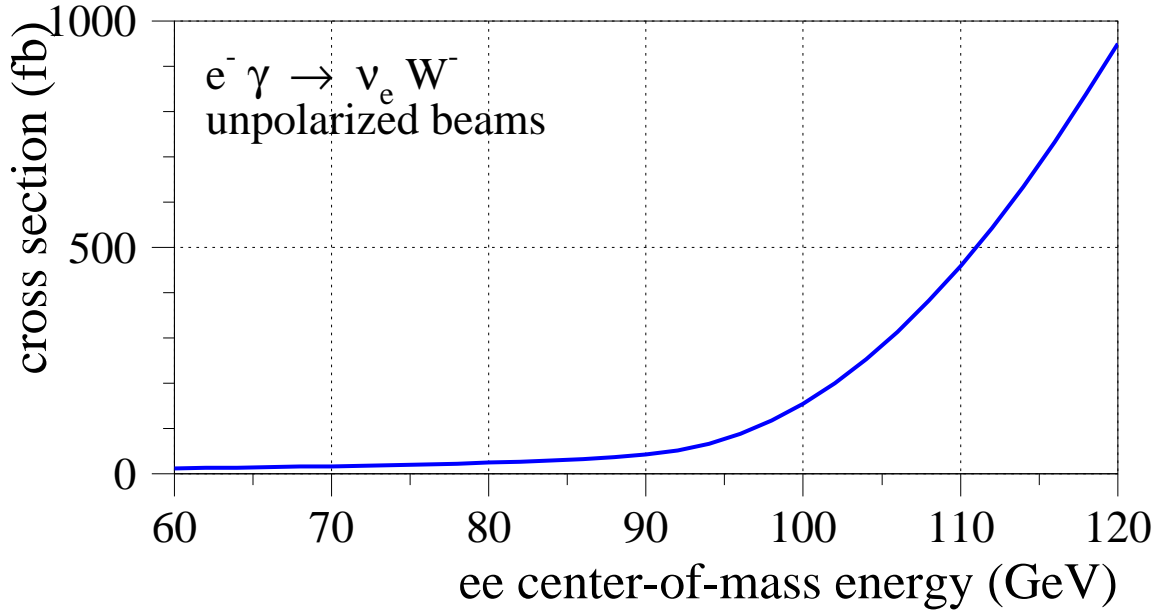


Figure 19: The rise of the cross section for $e^- \gamma \rightarrow \nu W^-$ as a function of $E_{CM}(e^- e^-)$.

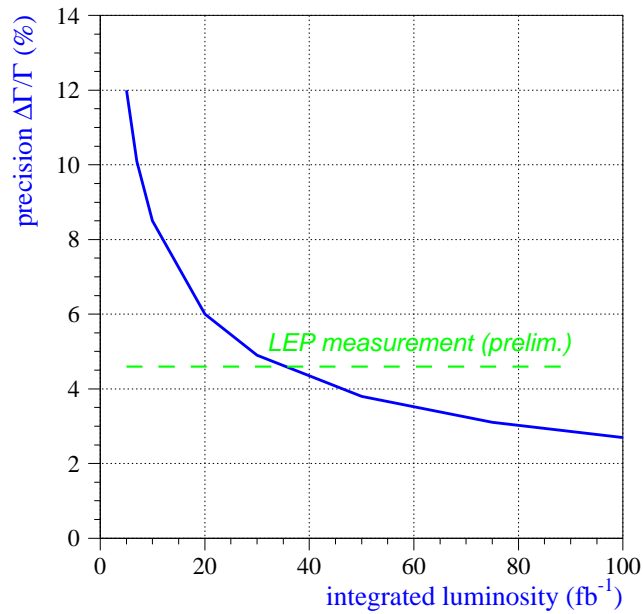


Figure 20: The sensitivity with which Γ_W might be measured at in $e^- \gamma$ collisions, as a function of the integrated luminosity available.

that could be gained earlier at a dedicated facility such as CLICHE could be exploited at the higher energies attainable at a TeV-scale linear collider, and eventually also at a multi-TeV collider such as CLIC [65].

Clearly the exploratory studies on machine and physics presented here need to be pursued with more detailed analyses. Ideas exist on the machine side that may lead to an increased luminosity for CLICHE. Also, it is possible that the number of lasers needed could be reduced by using recirculating laser pulses in the interaction region. If the Higgs proves to be heavier than about 125 GeV, one could also think of upgrading the input beam energy to CLIC 1.

We recall that CLICHE is just one of several possible options for doing physics with CLIC 1, many of which are more conventional and deserving serious study. However, we consider CLICHE to be a very attractive option for a project that could simultaneously validate and test all components of the CLIC technology for accelerating high-energy beams and can give important scientific output, covering a unique facet of the study of the Higgs boson, whose study will be central to physics at the high-energy physics frontier over the next decade or two.

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